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# Structure of tellurite glasses—effects of $\mathbf{K}_{2} \mathrm{O}$ or $\mathbf{P}_{\mathbf{2}} \mathrm{O}_{\mathbf{5}}$ additions studied by diffraction 

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#### Abstract

Neutron and x-ray diffraction experiments of high resolving power with neutrons from a spallation source and high-energy photons from a synchrotron have been performed on compositional series of binary tellurite glasses with additions of $\mathrm{K}_{2} \mathrm{O}$ or $\mathrm{P}_{2} \mathrm{O}_{5}$ (max. 16 or $32 \mathrm{~mol} \%$ ). Since the $\mathrm{P}-\mathrm{O}$ bond lengths do not interfere with the $\mathrm{Te}-\mathrm{O}$ peaks the $\mathrm{Te}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ correlations are approximated by Gaussian fitting of the x-ray and neutron correlation functions up to lengths of 0.28 nm . In the case of $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses reasonable assumptions are made for the $\mathrm{K}-\mathrm{O}$ first-neighbour peaks. $\mathrm{Te}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ coordination numbers are four and five for the glasses of compositions close to pure $\mathrm{TeO}_{2}$ which indicates formation of a three-dimensional network of cornerconnected $\mathrm{TeO}_{4}$ trigonal bipyramids. The tellurite network groups are $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{3}$ units in $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses and $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{5}$ units in $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses. Additional $\mathrm{Te}-\mathrm{O}$ neighbours found at $0.23 \mathrm{~nm}<r<0.26 \mathrm{~nm}$ for $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses suggest the existence of $\mathrm{TeO}_{3+1}$ units and those found at $0.23 \mathrm{~nm}<r<0.29 \mathrm{~nm}$ for the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses indicate the existence of distorted $\mathrm{TeO}_{6}$ polyhedra. Tellurite networks are flexible to form the appropriate coordination environments for quite different ions or groups of opposite charge such as $\mathrm{K}^{+}$ions and $\left(\mathrm{PO}_{4 / 2}\right)^{-}$tetrahedra where change of the $\mathrm{TeO}_{n}$ network units provides the needed number of oxygen neighbours.


## 1. Introduction

Tellurite glasses are attracting a lot of attention because of their high refractive index (see e.g. [1] and the literature therein), anomalous partial dispersion in the visible light region [2], high acousto-optical figure of merit [3], high third-order non-linear susceptibility [4, 5], good lasing [6] and optical amplifying properties [7], as well as good transmittance in the nearinfrared region (NIR) [8]. In some specific cases these properties are combined with good chemical and crystallization stability [9].

The main peculiarity of the structure of tellurite crystals, melts and glasses is the presence of a sterically active lone pair of the $5 \mathrm{~s}^{2}$ electrons (LPE) at the tellurium(IV) atom. For example, the LPE causes an enormous variability of the Te-O bond lengths in tellurite crystals [10, 11]. Actually, it is often difficult to separate the oxygen atoms in tellurite structures into the classical bridging and non-bridging types only. Intermediate oxygen atoms, called semi-bridging [12], can be found in these structures too. Another characteristic is the temperature-induced, chargeindependent change of the $\mathrm{Te}-\mathrm{O}$ coordination number in tellurite melts [13] which causes a fast depolymerization of their network on heating and which predetermines their 'fragility' [14]. The structural variability of tellurite materials could be used to tailor the physical properties of glasses as well as their thermal and chemical stability parameters. This possibility justifies the steady interest in structural investigations of tellurite glasses.

The aim of the present contribution is to study the short-range order (SRO) of binary tellurite glasses using x-ray and neutron diffraction techniques. The oxides $\mathrm{K}_{2} \mathrm{O}$ and $\mathrm{P}_{2} \mathrm{O}_{5}$ are chosen as second components of the glasses because $\mathrm{K}_{2} \mathrm{O}$ is a typical network modifier (or Lewis base), but $\mathrm{P}_{2} \mathrm{O}_{5}$ represents a typical network former (or Lewis acid). Both systems, $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ and $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$, possess relatively large glass-forming regions [15]. Moreover, the $\mathrm{Te}-\mathrm{O}, \mathrm{K}-\mathrm{O}$ and $\mathrm{P}-\mathrm{O}$ distances differ clearly, which simplifies the structural evaluations. The $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ system is widely studied with diffraction [16-18] and spectroscopic [18-22] methods. But not much is known about the structural behaviour in the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ system. Some diffraction work was performed on tellurite glasses of small $\mathrm{P}_{2} \mathrm{O}_{5}$ content [23].

## 2. Experimental details

Three samples of the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ system and six samples of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ system were prepared with compositions listed in table 1. The glasses were melted in covered gold crucibles for 1.5 h at $800^{\circ} \mathrm{C}$ for the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ samples and at $850-900^{\circ} \mathrm{C}$ for the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ samples. The melts were cast into cold brass moulds. The glasses were annealed at $300^{\circ} \mathrm{C}$ and, subsequently, cooled down slowly. The sample with $2 \mathrm{~mol} \% \mathrm{P}_{2} \mathrm{O}_{5}$ was pressed on a cold copper block to avoid crystallization. Mass densities were measured by Archimedes' principle. Nominal compositions were used for the structural analysis. Densities and compositions are given in table 1. From the area of the P-O peaks with coordination numbers, $N_{\mathrm{PO}}$, of $\sim 3.5$ (four is expected) it reveals that the real $\mathrm{P}_{2} \mathrm{O}_{5}$ contents of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses were reduced during melting (cf section 3.4). The final $\mathrm{P}_{2} \mathrm{O}_{5}$ fractions are also given in table 1. The new compositions were chosen to fit with numbers $N_{\mathrm{PO}}$ of four. Also the sums of bond valencies were checked for the different $\mathrm{Te}-\mathrm{O}$ distances of the $\mathrm{Te}(\mathrm{IV})$ atoms to give reasonable numbers (cf section 3.3).

The neutron diffraction experiments were performed at the GEM diffractometer of the spallation source ISIS of the Rutherford Appleton Laboratory (Chilton/UK). The glassy material was crushed and loaded into vanadium cylinders 8.3 mm in diameter and with wall thickness of only 0.025 mm . The beam size was $12 \times 40 \mathrm{~mm}^{2}$. The duration of the data collection was at least 3 h for each sample. A 6 mm vanadium rod was used to obtain the


Figure 1. Differential scattering cross-sections, $\mathrm{d} \sigma / \mathrm{d} \Omega$, of sample tep 14 obtained by neutron diffraction. The data shown of four detector groups of the GEM instrument result after finishing all corrections and normalization. These data are used to obtain the final structure factor.

Table 1. Compositions and densities of the tellurite glasses studied. Glasses with $\mathrm{K}_{2} \mathrm{O}$ are named tek; those with $\mathrm{P}_{2} \mathrm{O}_{5}$ are given labels tep.

| Sample <br> label | $\mathrm{K}_{2} \mathrm{O}$ or $\mathrm{P}_{2} \mathrm{O}_{5}$ content |  | $c\left(\mathrm{M}_{z} \mathrm{O}\right)$ | Mass density$\left(\mathrm{g} \mathrm{~cm}^{-3}\right)$ | Number density of atoms ( $\mathrm{nm}^{-3}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | As badged | Corrected |  |  |  |
| tek08 | 0.08 | - | 0.080 | 5.083(2) | 59.49 |
| tek12 | 0.12 | - | 0.120 | 4.850 (2) | 57.74 |
| tek16 | 0.16 | - | 0.160 | 4.609(2) | 55.84 |
| tep02 | 0.02 | - | 0.092 | 5.493(2) | 63.98 |
| tep08 | 0.08 | - | 0.303 | 5.295(2) | 66.93 |
| tep14 | 0.16 | 0.14 | 0.449 | 4.958(2) | 67.65 |
| tep19 | 0.24 | 0.19 | 0.540 | 4.739(2) | 68.68 |
| tep 27 | 0.32 | 0.27 | 0.649 | 4.339(2) | 68.86 |
| tep32 | 0.40 | 0.32 | 0.702 | 4.158(2) | 69.62 |

incident energy spectrum which is needed for data normalization in the time-of-flight regime. The diffraction data were corrected using standard procedures for container and background scattering, attenuation, multiple scattering and inelasticity effects [24]. Finally, the differential scattering cross-sections, $\mathrm{d} \sigma / \mathrm{d} \Omega$, collected in the detector groups $2,3,4$, and 5 are used. The corresponding functions of sample tep 14 are shown in figure 1 . An unusual feature exists in the data for $Q>80,150,270$, and $400 \mathrm{~nm}^{-1}$, respectively ( $Q$ is the momentum transfer with $Q=4 \pi / \lambda \cdot \sin \theta, \lambda$-radiation wavelength, $2 \theta$-scattering angle). The strong decay is due to resonance effects of Te nuclei for epithermal neutrons of 2.3 eV . Another spurious but small decay visible in the data range $200 \mathrm{~nm}^{-1}<Q<400 \mathrm{~nm}^{-1}$ of detector group 5 was removed by an empirical function. For composing the final Faber-Ziman structure factors $S_{N}(Q)$ [25] the data of groups 2, 3 and 4 were adjusted to those of group 5.

The x-ray diffraction experiments were performed at the BW5 wiggler beamline at DORIS III of Deutsches Elektronen-Synchrotron(Hamburg). An incident photon energy of 122.7 keV $(\lambda=0.0101 \mathrm{~nm})$ was chosen for the experiments. The beam size was $1 \times 4 \mathrm{~mm}^{2}$. Exact absorption corrections are difficult because the diameter of 1.5 mm of the silica capillaries (with wall thickness of 0.01 mm ) containing the glassy powder exceeds the beam width.


Figure 2. X-ray scattering intensities of sample tep14 after finishing all corrections and normalization. The solid-line function is the structure-independent scattering which is the sum of the compositional average of squares of atomic scattering amplitudes $\left\langle f^{2}(Q)\right\rangle$ and of the Compton scattering. The quotient of both functions is shown in the upper right section to visualize small normalization deficits in the high- $Q$ range.

The scattering angles are small $\left(2 \theta=28^{\circ}\right.$ for $\left.Q_{\max }=300 \mathrm{~nm}^{-1}\right)$ and the transmission coefficients are greater than 0.9 so that absorption is independent of the angle $\theta$. The electronic energy window of the solid-state Ge detector was chosen to pass the elastic line and the full Compton peak but no fluorescence radiation. Dead-time corrections were made with parameter $\tau=1.08 \mu \mathrm{~s}$ [26] and a fraction of 0.91 of incident photons is polarized horizontally. Corrections were made for background, container scattering, polarization and absorption. Subsequently, scattering intensities were normalized to the structure-independent scattering functions which were obtained from the tabulated atomic elastic scattering factors [27] and atomic Compton scattering data [28]. Figure 2 shows the scattering intensities of sample tep 14 after normalization to the corresponding structure-independent scattering. A quotient of both functions is shown in the upper right section of the figure. The quality of data is satisfactory to obtain an excellent normalization. An empirical correction with a smooth function was used in the range of $Q>\sim 220 \mathrm{~nm}^{-1}$ that makes the scattering intensity oscillate around the structureindependent scattering. Deficits in the calculation of the Compton fraction, uncertainties of the chemical compositions, errors in the instrument calibration and instabilities of beam position and of monitor efficiencies can cause the deviations. Finally, the Faber-Ziman structure factors, $S_{X}(Q)$, are calculated [25, 29].

## 3. Results

### 3.1. Structure factors and correlation functions

The neutron and x-ray structure factors shown in figures 3(a), (b) are weighted with $Q$ to make visible the oscillations in the high- $Q$ range. If compared with the other series only small changes of the corresponding functions are visible for the samples tek08, tek12 and tek16. But the $\mathrm{K}_{2} \mathrm{O}$ contents of the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses are small if compared with the $\mathrm{P}_{2} \mathrm{O}_{5}$ contents of the other samples. For comparison of the structural effects of second oxides it is better to consider the fractions $c\left(\mathrm{M}_{z} \mathrm{O}\right)$ with $\mathrm{M}=\mathrm{K}$ or P as given in table 1 . Specific features of the structure factors of the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses are a double first peak in the $S_{N}(Q)$ data and a prepeak in


Figure 3. Weighted structure factors of the samples studied: (a) neutron data and (b) x-ray data. Upper functions are shifted for clearness of the plot.
the $S_{X}(Q)$ data whose height increases with increasing $\mathrm{K}_{2} \mathrm{O}$ content. Such features were also found by other authors [16-18]. On the other hand, strong systematic changes accompanying the growing $\mathrm{P}_{2} \mathrm{O}_{5}$ content exist in the structure factors of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ series. The diffraction data of sample tep02 are similar to those reported by Neov et al [23]. Different from most earlier work [16-18] greater $Q$-ranges were realized in our experiments. The better resolving power and the combination of neutron and x -ray data help to extract more details of the $\mathrm{Te}-\mathrm{O}$ first-neighbour peaks, and thus about the $\mathrm{TeO}_{n}$ structural units. The data of high $Q$-values are important to resolve detailed information of the narrow peak components of the covalent bonds. The truncation effects of $Q_{\max }$ in the Fourier transformations (FT) are reduced evidently with $Q_{\max }$ of 400 or $280 \mathrm{~nm}^{-1}$ for the neutron or x-ray data. The real-space correlation functions, $T(r)$, are calculated with

$$
\begin{equation*}
T(r)=4 \pi r \rho_{0}+2 / \pi \int_{0}^{Q_{\max }} Q[S(Q)-1] M(Q) \sin (Q r) \mathrm{d} Q . \tag{1}
\end{equation*}
$$

Here $\rho_{0}$ is the number density of atoms (table 1 ). The function $M(Q)$ is introduced to damp spurious features such as ripples caused by noise and by termination of the Fourier integral at $Q_{\max }$. The function $M(Q)$ used is $M(Q)=\sin \left(\pi Q / Q_{\max }\right) /\left(\pi Q / Q_{\max }\right)$ [30]. The resulting


Figure 4. Correlation functions of all samples obtained with Fourier transformation using damping and $Q_{\text {max }}$ of $400 \mathrm{~nm}^{-1}$ for the neutron data (a) and $280 \mathrm{~nm}^{-1}$ for the x-ray data (b). The $T(r)$ functions of the different samples are plotted in the same order as in figure 3. Upper functions are shifted for clearness of the plot.
$T(r)$ functions are compared in figure 4. The peak broadening is already a small effect with $Q_{\text {max }}$ of $400 \mathrm{~nm}^{-1}$. Thus, the neutron $T_{N}(r)$ functions show nearly all details of peaks of the glass structure which could be extracted. The $\mathrm{P}-\mathrm{O}$ peaks are narrower in the $T_{N}(r)$ functions obtained without damping but the corresponding satellite oscillations make peak fits more difficult. Hence, $T(r)$ functions obtained with damping as shown in figure 4 are used in the peak fitting. A good agreement between the $T(r)$ functions obtained without damping and the corresponding model $T(r)$ functions calculated with the final peak parameters was achieved in most cases, as well. But a few of the $T(r)$ functions obtained without damping show some unphysical features and, therefore, they are not used and not shown.

### 3.2. Gaussian fitting of the first-neighbour peaks

The height of the $\mathrm{P}-\mathrm{O}$ peak of bond lengths of $\sim 0.155 \mathrm{~nm}$ grows continuously with the $\mathrm{P}_{2} \mathrm{O}_{5}$ content. The fit of this peak is made by a single Gaussian function. A sharp Te-O peak follows at $\sim 0.19 \mathrm{~nm}$ which is accompanied by a long tail extending to 0.24 nm (cf figure 4). Other distances are not expected in this range. Thus, clear information is obtained for the

Table 2. Parameters resulting from Gaussian fitting of the $\mathrm{Te}-\mathrm{O}, \mathrm{K}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ first-neighbour peaks of the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses. Numbers in parenthesis give the uncertainty in the last digit. The parameters of the $\mathrm{K}-\mathrm{O}$ peak are fixed identical for all three samples of this series as given for tek08. The total Te-O coordination numbers take into account only the bonds with lengths less than $0.23 \mathrm{~nm} . N_{\text {short }}$ and $N_{\text {long }}$ contain bond lengths of 0.19 and $0.20-0.23 \mathrm{~nm}$, respectively.

| Sample | Atom pair | Peak parameters |  |  | Total coordination number | $N_{\text {short }}$ | $N_{\text {long }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $N_{i j}$ | $r_{i j}(\mathrm{~nm})$ | $\Delta r_{i j}(\mathrm{~nm})$ |  |  |  |
| tek08 | $\mathrm{Te}-\mathrm{O}$ | 1.90 | 0.189(1) | 0.013(2) | 3.90(10) | 1.90(10) | 2.00(20) |
|  |  | 1.05 | $0.203{ }^{\text {a }}$ | 0.018(3) |  |  |  |
|  |  | 0.95 | $0.220^{\text {a }}$ | 0.027(4) |  |  |  |
|  |  | 0.60 | $0.255^{\text {a }}$ | $0.028^{\text {a }}$ |  |  |  |
|  |  | 0.40 | $0.280^{\text {a }}$ | $0.030^{\text {a }}$ |  |  |  |
|  | K-O | $3.00^{\text {a }}$ | $0.267^{\text {a }}$ | $0.015^{\text {a }}$ |  |  |  |
|  |  | $4.00^{\text {a }}$ | $0.288^{\text {a }}$ | $0.035^{\text {a }}$ |  |  |  |
|  | $\mathrm{O}-\mathrm{O}$ | 5.04 | 0.282 | 0.036 |  |  |  |
| tek12 | Te-O | 1.95 | 0.188(1) | 0.015(2) | 3.85(10) | 1.95 (10) | 1.90 (20) |
|  |  | 0.95 | $0.203{ }^{\text {a }}$ | 0.017(3) |  |  |  |
|  |  | 0.95 | $0.220^{\text {a }}$ | 0.027(4) |  |  |  |
|  |  | 0.50 | $0.255^{\text {a }}$ | $0.028^{\text {a }}$ |  |  |  |
|  |  | 0.30 | $0.280^{\text {a }}$ | $0.030^{\text {a }}$ |  |  |  |
|  | $\mathrm{O}-\mathrm{O}$ | 5.10 | 0.284 | 0.036 |  |  |  |
| tek16 | Te-O | 1.90 | 0.189(1) | 0.014(2) | 3.75(10) | 1.85 (10) | 1.90 (20) |
|  |  | 0.85 | $0.203{ }^{\text {a }}$ | 0.018(3) |  |  |  |
|  |  | 1.00 | $0.220^{\text {a }}$ | 0.032(4) |  |  |  |
|  |  | 0.40 | $0.255^{\text {a }}$ | $0.028^{\text {a }}$ |  |  |  |
|  |  | 0.33 | $0.280^{\text {a }}$ | $0.030^{\text {a }}$ |  |  |  |
|  | $\mathrm{O}-\mathrm{O}$ | 4.46 | 0.284 | 0.034 |  |  |  |

${ }^{\mathrm{a}}$ These values are fixed in the fits.

Te-O bond lengths. From knowledge of the structure of the related crystals $\mathrm{P}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ [31] and $\mathrm{P}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ [32] we can assume that except for the short $\mathrm{P}-\mathrm{O}$ bonds other than $\mathrm{Te}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ distances do not exist for lengths less than $\sim 0.29 \mathrm{~nm}$ (cf section 4.3). An unequivocal fit of $\mathrm{Te}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ distances is possible in this $r$-range because two data sets, the $T_{N}(r)$ and $T_{X}(r)$ functions, are available. For the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses, additionally, a broad peak of $\mathrm{K}-\mathrm{O}$ distances is expected at $\sim 0.275 \mathrm{~nm}$ which superposes with the lengths of the $\mathrm{O}-\mathrm{O}$ edges of the $\mathrm{TeO}_{n}$ groups and possible longer $\mathrm{Te}-\mathrm{O}$ distances. However, the contribution of $\mathrm{K}-\mathrm{O}$ distances is small in both $T(r)$ functions. Fits with fixed parameters of the $\mathrm{K}-\mathrm{O}$ first-neighbour peaks are justified. Approximate parameters taken from earlier diffraction work ( $\mathrm{KPO}_{3}$ glass [33]) and from structures of K tellurite crystals [34] are used for the $\mathrm{K}-\mathrm{O}$ peak. The fixed parameters are given below in table 2.

As already realized in our earlier diffraction work of tellurite glasses $[35,36]$ the $\mathrm{Te}-$ O first-neighbour peak is fitted with three Gaussian functions. A few possible longer $\mathrm{Te}-\mathrm{O}$ distances are approximated with broad Gaussian functions with fixed distances of 0.240 ( 0.255 ) and 0.280 nm . The $\mathrm{O}-\mathrm{O}$ peak of $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses is approximated with a single Gaussian function at $\sim 0.28 \mathrm{~nm}$. This approach was successful in the analysis of the $\mathrm{V}, \mathrm{Zn}$ and Nb tellurite glasses studied earlier [35, 36]. In the case of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses, additionally, a sharp peak of $\mathrm{O}-\mathrm{O}$ distances occurs at $\sim 0.252 \mathrm{~nm}$ (cf figure 4(a)) which belongs to the edges of the $\mathrm{PO}_{4}$ tetrahedra. Thus, two or three Gaussian functions are used for the $\mathrm{O}-\mathrm{O}$ contribution in the case of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses. The broad Gaussian functions used form


Figure 5. Correlation functions in the range of the first-neighbour peaks of the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses (dotted lines): (a) neutron and (b) x-ray data. The model $T(r)$ functions are given as thick solid lines; the partial correlations are given as thin solid lines $(\mathrm{Te}-\mathrm{O})$, dashed lines $(\mathrm{K}-\mathrm{O})$ and dashdotted lines ( $\mathrm{O}-\mathrm{O}$ ).
rather continuous $\mathrm{Te}-\mathrm{O}, \mathrm{O}-\mathrm{O}$ and $\mathrm{K}-\mathrm{O}$ distance distributions. The analysis of distributions is stopped at $\sim 0.29 \mathrm{~nm}$. Most of the Gaussian functions do not form well resolved peaks and, thus, should not be interpreted to represent specific types of bonds. An exception was the differentiation made in $[35,36]$ for short and long Te-O bonds of $\sim 0.19$ and $\sim 0.21 \mathrm{~nm}$ of the $\mathrm{TeO}_{n}$ structural groups. The fractions of these bonds confirm the existence of $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{3}$ units as trigonal bipyramids (tbps) and trigonal pyramids (tps). Here and below notations concerning the $\mathrm{Te}-\mathrm{O}$ coordination state are used in the classical sense, i.e. regarding only bond lengths less than 0.23 nm . A similar character of the $\mathrm{Te}-\mathrm{O}$ peak is visible for the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses and for sample tep02 (cf figure 4). The dominance of a narrow component at $\sim 0.19 \mathrm{~nm}$ is lost for the $\mathrm{Te}-\mathrm{O}$ peaks of the other $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses due to increasing fractions of distances greater than 0.20 nm .

Gaussian fitting is performed to the $T_{N}(r)$ and $T_{X}(r)$ data simultaneously. The model $T(r)$ functions fit the experimental data up to lengths of 0.28 nm . The effects caused by termination of FT at $Q_{\text {max }}$ are taken into account by convolution of the model Gaussian functions with peak functions, $P_{i j}(r)$, which simulate the $Q$-window and damping used in equation (1) [37, 38]. The parameters are the coordination numbers, $N_{i j}$, the mean distances, $r_{i j}$, and the peak widths (full widths at half maximum), $\Delta r_{i j}$, for pairs of atomic species $i$ and $j$. Least-squares fits are performed using the Marquardt algorithm [39]. The constraints and parameters fixed in the fits have been varied several times to find the optimum set of Gaussian functions that is needed to approximate the experimental $T(r)$ functions. Starting parameters for the Te-O peak are chosen as reported before $[35,36]$.

### 3.3. Fit results of the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses

The successful fits of the $T(r)$ functions of the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses are shown in figure 5 and the corresponding parameters of the Gaussian functions are given in table 2. The resulting parameters show that with decreasing $\mathrm{K}_{2} \mathrm{O}$ content and approaching pure $\mathrm{TeO}_{2}$ glass $N_{\mathrm{TeO}}$ approaches four, which indicates the existence of $\mathrm{TeO}_{4}$ units. $\mathrm{TeO}_{3}$ units are formed with increasing $\mathrm{K}_{2} \mathrm{O}$ content. But the clear separation into a narrow and a broad peak component as was successful in the earlier work $[35,36]$ is not well developed. If the Te-O peak is assumed to be formed of two components, the first with distances of 0.19 nm and the second with


Figure 6. Correlation functions in the range of the first-neighbour peaks of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses (dotted lines): (a) neutron and (b) x-ray data. The model $T(r)$ functions are given as thick solid lines; the partial correlations are given as dashed lines ( $\mathrm{P}-\mathrm{O}$ ), thin solid lines $(\mathrm{Te}-\mathrm{O})$ and dashdotted lines $(\mathrm{O}-\mathrm{O})$
distances ranging from 0.20 to 0.22 nm , equal fractions of short $\mathrm{Te}-\mathrm{O}_{\mathrm{eq}}$ and longer $\mathrm{Te}-\mathrm{O}_{\mathrm{ax}}$ bonds are found which is typical for $\mathrm{TeO}_{4}$ tbp units (cf table 2, illustrations of the units in section 4.2). The increase of the fraction of short $\mathrm{Te}-\mathrm{O}$ bonds expected as an accompanying effect of the increase of the number of $\mathrm{TeO}_{3}$ at the expense of $\mathrm{TeO}_{4}$ units reported for glasses of higher modifier content [35,36] is not significant for our short series of $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses.

Supposing the uncertainty of the assumptions made for the model K-O distance peak is small, so the fit yields clear indications for the existence of Te-O distances beyond typical bond lengths ( $>0.23 \mathrm{~nm}$ ). Te-O distances of 0.255 nm have to be taken into account which is especially needed to fit the x -ray results (figure $5(\mathrm{~b})$ ). Such distances can belong to $\mathrm{TeO}_{3+1}$ units as the additional longer bond. But also the Te atoms in $\mathrm{TeO}_{4}$ units can possess additional oxygen neighbours, for example, forming distorted $\mathrm{TeO}_{6}$ octahedra as are known of the $\mathrm{TeO}_{2}$ polymorphs [40-42] (cf section 4.2). A next small contribution is assumed at 0.280 nm but here the separation of different partials becomes already questionable. The sums of bond valencies, $S_{\mathrm{bv}}$, of the $\mathrm{TeO}_{n}$ units [43] with $i$ running from 1 to 5 with the $i$ th $\mathrm{Te}-\mathrm{O}$ distances $r_{i}$ and weights $N_{i}$ (table 2) are checked with

$$
\begin{equation*}
S_{\mathrm{bv}}=\Sigma_{i} N_{i} 1.333\left(r_{i} / 0.1854\right)^{-5.2} \tag{2}
\end{equation*}
$$

The $S_{\mathrm{bv}}$ result in 3.8-3.9 (four is expected for Te (IV) atoms) which confirms the fit approach used. The total number of oxygen neighbours up to distances of 0.28 nm obtained in the fits decreases from 4.9 for sample tek 08 to 4.6 for sample tek 16 .

### 3.4. Fit results of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses

The fit results of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses are shown in figure 6 and the corresponding parameters of the Gaussian functions are given in table 3. A first analysis of the $T(r)$ functions using the nominal compositions (table 1) has led to unexpected small P-O coordination numbers, $N_{\mathrm{PO}}$, of 3.5-3.6 accompanied by high $N_{\text {TeO }}$ numbers up to $\sim 6$. Loss of volatile $\mathrm{P}_{2} \mathrm{O}_{5}$ could explain this behaviour. Therefore, the $\mathrm{P}_{2} \mathrm{O}_{5}$ contents are varied for samples tep14, tep19, tep27, and

Table 3. Parameters resulting from Gaussian fitting of the Te-O, $\mathrm{P}-\mathrm{O}$, and $\mathrm{O}-\mathrm{O}$ first-neighbour peaks of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses. The numbers in parenthesis give the uncertainty in the last digit.

| Sample | Te-O coordination |  |  | Atom pair | $\mathrm{P}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ coordination |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $N_{\text {TeO }}$ | $r_{\text {TeO }}(\mathrm{nm})$ | $\Delta r_{\text {TeO }}(\mathrm{nm})$ |  | $N_{i j}$ | $r_{i j}(\mathrm{~nm})$ | $\Delta r_{i j}(\mathrm{~nm})$ |
| tep02 | 1.90 | 0.190(1) | 0.014(2) | P-O | $4.00^{\text {a }}$ | 0.155(1) | 0.007(5) |
|  | 1.35 | 0.206 | 0.024 |  |  |  |  |
|  | 0.75 | $0.220^{\text {a }}$ | 0.035 | O-O | 0.45 | $0.252^{\text {a }}$ | 0.017 |
|  | 0.35 | $0.240^{\text {a }}$ | $0.030^{\text {a }}$ |  | 2.39 | 0.275 | 0.032 |
|  | 0.95 | $0.280^{\text {a }}$ | $0.030^{\text {a }}$ |  | 2.53 | 0.280 | $0.040^{\text {a }}$ |
| tep08 | 1.85 | 0.190(1) | 0.014(2) | P-O | $4.00^{\text {a }}$ | 0.154(1) | 0.011(3) |
|  | 1.40 | 0.206 | 0.022 |  |  |  |  |
|  | 0.90 | $0.220^{\text {a }}$ | 0.030 | $\mathrm{O}-\mathrm{O}$ | 0.80 | $0.252^{\text {a }}$ | 0.015 |
|  | 0.40 | $0.240^{\text {a }}$ | $0.030^{\text {a }}$ |  | 2.20 | 0.266 | 0.030 |
|  | 1.00 | $0.280^{\text {a }}$ | $0.030^{\text {a }}$ |  | 3.40 | 0.293 | $0.040^{\text {a }}$ |
| tep14 | 1.90 | 0.191(1) | 0.017(2) | P-O | $4.00^{\text {a }}$ | 0.154(1) | 0.011(2) |
|  | 1.33 | 0.206 | 0.025 |  |  |  |  |
|  | 0.95 | $0.218^{\text {a }}$ | 0.029 | $\mathrm{O}-\mathrm{O}$ | 1.70 | $0.252^{\text {a }}$ | 0.019 |
|  | 0.48 | $0.240^{\text {a }}$ | $0.030^{\text {a }}$ |  | 1.86 | 0.269 | 0.028 |
|  | 0.87 | $0.280^{\text {a }}$ | $0.030^{\text {a }}$ |  | 3.54 | 0.294 | $0.040^{\text {a }}$ |
| tep19 | 1.55 | 0.191(1) | 0.014(2) | P-O | $4.00^{\text {a }}$ | 0.154(1) | 0.011(2) |
|  | 1.85 | 0.206 | 0.024 |  |  |  |  |
|  | 0.91 | $0.218^{\text {a }}$ | 0.033 | $\mathrm{O}-\mathrm{O}$ | 1.72 | $0.252^{\text {a }}$ | 0.016 |
|  | 0.55 | $0.240^{\text {a }}$ | $0.030^{\text {a }}$ |  | 4.26 | 0.278 | 0.040 |
|  | 0.88 | $0.280^{\text {a }}$ | $0.030^{\text {a }}$ |  |  |  |  |
| tep27 | 2.10 | 0.190(1) | 0.018(2) | $\mathrm{P}-\mathrm{O}$ | $4.00^{\text {a }}$ | 0.154(1) | 0.013(2) |
|  | 1.66 | 0.212 | 0.022 |  |  |  |  |
|  | 0.70 | $0.220^{\text {a }}$ | 0.037 | $\mathrm{O}-\mathrm{O}$ | 2.23 | $0.252^{\text {a }}$ | 0.017 |
|  | 0.50 | $0.240^{\text {a }}$ | $0.030^{\text {a }}$ |  | 1.78 | 0.275 | 0.038 |
|  | 0.80 | $0.280^{\text {a }}$ | $0.030^{\text {a }}$ |  | 1.91 | 0.280 | 0.040 |
| tep32 | 2.00 | 0.190(1) | 0.017(2) | $\mathrm{P}-\mathrm{O}$ | $4.00^{\text {a }}$ | 0.154(1) | 0.013(2) |
|  | 1.80 | 0.212 | 0.021 |  |  |  |  |
|  | 0.80 | $0.220^{\text {a }}$ | 0.035 | $\mathrm{O}-\mathrm{O}$ | 2.70 | $0.252^{\text {a }}$ | 0.019 |
|  | 0.40 | $0.240^{\text {a }}$ | $0.030^{\text {a }}$ |  | 2.16 | 0.276 | 0.039 |
|  | 0.80 | $0.280^{\text {a }}$ | $0.030^{\text {a }}$ |  | 1.78 | 0.291 | 0.042 |

[^0]tep32 and the corresponding $N_{\mathrm{PO}}$ numbers are determined. Finally, those compositions are chosen for which $N_{\mathrm{PO}}$ equals four. The change of $\mathrm{P}_{2} \mathrm{O}_{5}$ content of sample tep 02 is negligible. A neutron diffraction experiment was not successful for sample tep08 and, thus, an improvement of the corresponding glass composition is not possible. In addition to the three Gaussian functions used to approximate the $\mathrm{Te}-\mathrm{O}$ bonds also two further peaks with $\mathrm{Te}-\mathrm{O}$ distances of 0.240 and 0.280 nm are used. The sums $S_{\text {bv }}$ calculated according to equation (2) give values very close to the expected number of four. This behaviour confirms the final $\mathrm{P}_{2} \mathrm{O}_{5}$ contents used in the data analyses. $S_{\text {bv }}$ values of four are also obtained for the $\mathrm{TeO}_{n}$ units of the related crystal structures [31,32]. The fits shown in figure 6 are not fully successful for distances ranging from 0.21 to 0.23 nm . The origin of these small differences between the neutron and x-ray $T(r)$ functions could not be clarified. The total number of oxygens bonded to the Te atoms is four for sample tep02 and it increases up to 4.6 for the sample of highest $\mathrm{P}_{2} \mathrm{O}_{5}$ content studied ( $32 \mathrm{~mol} \%$ ). If the more distant oxygen atoms up to 0.28 nm are also taken into account the total $\mathrm{Te}-\mathrm{O}$ coordination numbers behave as constant at $\sim 5.7$ which gives support to the


Figure 7. Behaviour of the $\mathrm{Te}-\mathrm{O}$ coordination numbers of the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ and $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses studied and of $N_{\text {TeO }}$ values reported for tellurite glasses with $\mathrm{V}_{2} \mathrm{O}_{5}$ [35], ZnO and $\mathrm{Nb}_{2} \mathrm{O}_{5}$ [36] additions. Note that only typical bond lengths less than 0.23 nm are taken into account for the $N_{\mathrm{TeO}}$ presented. The $N_{\mathrm{TeO}}$ numbers are compared with those of some related crystal structures $\left(\mathrm{TeO}_{2}\right.$ [4042], $\mathrm{P}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ [31], $\mathrm{P}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ [32], $\mathrm{K}_{2} \mathrm{Te}_{4} \mathrm{O}_{9} \mathrm{~K}_{2} \mathrm{Te}_{2} \mathrm{O}_{5}$ [34], $\mathrm{TiTe}_{3} \mathrm{O}_{8}$ [50], $\mathrm{Cs}_{2} \mathrm{Te}_{2} \mathrm{O}_{5}$ [51], $\mathrm{K}_{2} \mathrm{TeO}_{3}$ [52], $\mathrm{Zn}_{2} \mathrm{Te}_{3} \mathrm{O}_{8}$ [53], $\mathrm{Nb}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ [54], $\mathrm{Nb}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ [55], $\mathrm{V}_{2} \mathrm{Te}_{2} \mathrm{O}_{9}$ [56]). Details are discussed in sections 4.2 and 4.3. The dashed, dotted and solid lines specify behaviour of $N_{\mathrm{TeO}}$ according to four models of changes of $\mathrm{TeO}_{n}$ groups. The models are described in the text.
existence of distorted $\mathrm{TeO}_{6}$ octahedra in the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses studied. The numbers of O atoms with typical bond lengths show an unusual increase. Please note that the sums $S_{\text {bv }}$ of the $\mathrm{Te}(\mathrm{IV})$ atoms are constant at four and independent of the $\mathrm{P}_{2} \mathrm{O}_{5}$ content. Increasing $\mathrm{Te}-\mathrm{O}$ bond lengths compensate for the increase of $N_{\text {TeO }}$.

The lengths of the $\mathrm{P}-\mathrm{O}$ bonds at 0.154 nm match those found for other phosphate glasses [44]. Widths $\Delta r_{\text {PO }}$ of this peak at $\sim 0.012 \mathrm{~nm}$ are typical values for single types of bonds, either $\mathrm{P}-\mathrm{O}_{\mathrm{B}}$ or $\mathrm{P}-\mathrm{O}_{\mathrm{T}}\left(\mathrm{O}_{\mathrm{B}}\right.$ bridging, $\mathrm{O}_{\mathrm{T}}$ terminal oxygen). Hence it follows that preferably isolated $\mathrm{PO}_{4}$ tetrahedra (no $\mathrm{P}-\mathrm{O}-\mathrm{P}$ bridges but only $\mathrm{P}-\mathrm{O}-\mathrm{Te}$ links) with four equivalent $\mathrm{P}-\mathrm{O}_{\mathrm{T}}$ bonds (bond valency of $\sim 1.25$ ) are spread in the tellurite network. Such behaviour of $\mathrm{PO}_{4}$ units is known for phosphate glasses of small $\mathrm{P}_{2} \mathrm{O}_{5}$ content [45, 46]. The component at 0.252 nm in the $\mathrm{O}-\mathrm{O}$ correlations increasing with the $\mathrm{P}_{2} \mathrm{O}_{5}$ content is caused by the edges of the $\mathrm{PO}_{4}$ tetrahedra. A precise determination of the number of edges is not possible due to the overlap with $\mathrm{O}-\mathrm{O}$ edge lengths of the $\mathrm{TeO}_{n}$ polyhedra.

## 4. Discussion

### 4.1. Changes of the $\mathrm{TeO}_{n}$ groups in dependence on different second oxides

The Te-O coordination numbers obtained in the diffraction experiments are plotted in figure 7 where also earlier results of $\mathrm{V}, \mathrm{Zn}$ and Nb tellurite glasses are shown [35, 36]. Also other authors [23,47-49] reported $\mathrm{Te}-\mathrm{O}$ coordination numbers of modified tellurite glasses obtained in diffraction experiments of high resolving power. Numbers $N_{\text {TeO }}$ are similar to our results. However, these $N_{\text {TeO }}$ are not shown in figure 7 because we do not want to mix results analysed in different ways. Please note that only $\mathrm{Te}-\mathrm{O}$ bonds of lengths less than 0.23 nm are taken into account for the $N_{\mathrm{TeO}}$ shown. Four of the samples studied possess only small fractions $c\left(\mathrm{M}_{z} \mathrm{O}\right)$ of second oxide. The corresponding $N_{\mathrm{TeO}}$ numbers tend to four in the compositional limit of a
glass of pure $\mathrm{TeO}_{2}$. In the opposite direction, with increasing $c\left(\mathrm{M}_{z} \mathrm{O}\right)$ fractions, the behaviour of $N_{\mathrm{TeO}}$ strongly depends on the atomic species M.

Figure 7 shows also the $N_{\text {TeO }}$ of related crystal structures. Analysis of the $\mathrm{TeO}_{n}$ units of these structures already reveals the problem: for presentation of the $N_{\text {TeO }}$ of the crystals all $\mathrm{TeO}_{n}$ polyhedra have been classified into units with $n=3,4$ and 5 taking into account only distances shorter than 0.23 nm . According to [12,57] these Te-O distances belong to 'strong' bonds. Some units possess longer $\mathrm{Te}-\mathrm{O}$ distances up to 0.26 nm ('medium' bond strength) which are called $\mathrm{TeO}_{n+m}$ units where $m$ indicates the number of 'medium' bonds. Finally, most Te-centred oxygen polyhedra are completed by O atoms in 'weak' bonds situated next to the LPE of the Te(IV) atom. These bonds possess greater lengths in an interval from 0.26 to 0.32 nm . For these distances a clear differentiation from $\mathrm{Te}-\mathrm{O}$ second neighbours is already difficult.

Analysis of our diffraction data of glasses results in continuous $T_{\mathrm{TeO}}(r)$ functions where five Gaussian functions have been used to approximate their shape. For the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ samples we have to assume a mixture of $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{3}$ units where, probably, the $\mathrm{TeO}_{3}$ can be called $\mathrm{TeO}_{3+1}$ units due to $\mathrm{Te}-\mathrm{O}$ 'medium' bonds approximated with the Gaussian peak at 0.255 nm . But some of these distances can also belong to $\mathrm{TeO}_{4}$ units and further differentiation of types of polyhedra is not possible from diffraction results. The total number of O neighbours including those of the Gaussian function at 0.28 nm is less than five and it decreases with increasing $\mathrm{K}_{2} \mathrm{O}$ content.

The $N_{\text {TeO }}$ numbers of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses increase to values greater than four with increasing $\mathrm{P}_{2} \mathrm{O}_{5}$ content. Mixtures of $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{5}$ units have to be assumed. The fraction of $\mathrm{Te}-\mathrm{O}$ bond lengths ranging from 0.20 to 0.22 nm exceeds that of lengths of $\sim 0.19 \mathrm{~nm}$. Clear differentiation into fractions $N_{\text {short }}$ and $N_{\text {long }}$ as made for the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses is not possible. Details of the conformations of $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{5}$ groups cannot be extracted. If the complete first-neighbour environments with distances up to 0.28 nm are taken into account, distorted $\mathrm{TeO}_{6}$ octahedra exist for all glasses of different $\mathrm{P}_{2} \mathrm{O}_{5}$ content. The existence of $\mathrm{Te}-\mathrm{O}$ first-neighbour distances ranging from 0.23 to 0.32 nm is also a fact for $\mathrm{TeO}_{n}$ groups in the glasses. Before more of the corresponding details of the glasses studied are discussed and compared with those of the related crystal structures (next sections) the general behaviour of the structural groups is considered.

For a general view it is useful to restrict the discussion to those $N_{\mathrm{TeO}}$ values which are determined as 'strong' bonds with lengths less than 0.23 nm . The numbers $N_{\mathrm{TeO}}$ can be related directly to the fractions of the different units. Therefore, it is sufficient to discuss the behaviour of $N_{\text {TeO }}$. Figure 7 shows the great variability of $\mathrm{TeO}_{2}$ forming structural units which also reveals its intermediate character forming binary glasses. The oxygen added does not simply disrupt network bridges. In dependence on the coordination preferences of the atomic species M of the second oxide $\mathrm{M}_{z} \mathrm{O}$ the number of terminal oxygens $\left(\mathrm{O}_{\mathrm{T}}\right)$ can be increased by changing some $\mathrm{TeO}_{4}$ having one $\mathrm{O}_{\mathrm{T}}$ to $\mathrm{TeO}_{3}$ units having two $\mathrm{O}_{\mathrm{T}}$ where the electron charge and new $\mathrm{Te}=\mathrm{O}$ double bond are delocalized on both $\mathrm{Te}-\mathrm{O}_{\mathrm{T}}$ bonds. The behaviour of $N_{\mathrm{TeO}}$ shown with the dashed-line function in figure 7 would be valid if a maximum of $\mathrm{TeO}_{4} \rightarrow \mathrm{TeO}_{3}$ transitions were realized (model A) where $N_{\mathrm{TeO}}$ is calculated with

$$
\begin{equation*}
N_{\mathrm{TeO}}=4-2 c\left(\mathrm{M}_{z} \mathrm{O}\right) / c\left(\mathrm{TeO}_{2}\right) \tag{3}
\end{equation*}
$$

From spectroscopic data of tellurite glasses modified with $\mathrm{Li}_{2} \mathrm{O}, \mathrm{Na}_{2} \mathrm{O}, \mathrm{BaO}$ and ZnO [58] this behaviour was suggested to be valid in the limit of small modifier additions. ${ }^{125} \mathrm{Te}$ nuclear magnetic resonance (NMR) spectroscopy has shown similar behaviour for tellurite glasses with $\mathrm{M}=\mathrm{La}, \mathrm{Na}, \mathrm{K}, \mathrm{Rb}, \mathrm{Cs}$ [22], $\mathrm{M}=\mathrm{Mg}, \mathrm{Zn}, \mathrm{Sr}, \mathrm{Ba}, \mathrm{Pb}[59]$ and $\mathrm{M}=\mathrm{Al}, \mathrm{Ga}$ [60]. Our diffraction results confirm this behaviour for tellurite glasses with ZnO [36] and $\mathrm{K}_{2} \mathrm{O}$ (this work). Actually,
the real $N_{\mathrm{TeO}}$ numbers are little greater than predicted by model A which means that also $\mathrm{TeO}_{4}$ with $\mathrm{O}_{\mathrm{T}}$ still exist. This fraction increases with further modifier additions [22, 58-60]. Four $\mathrm{O}_{\mathrm{T}}$ are formed for every oxygen added if model A is valid. Consequently, for $\mathrm{M}=\mathrm{Al}$ and Ga a behaviour according to model A is only advantageous if the $\mathrm{M}-\mathrm{O}$ coordination numbers are equal to six. In the process of increasing contents of $\mathrm{M}=\mathrm{Al}, \mathrm{Ga}$ mixed coordination states of the M sites were found $\left(\mathrm{AlO}_{4}, \mathrm{AlO}_{5}, \mathrm{AlO}_{6}\right.$ units [60]; $\mathrm{GaO}_{4}, \mathrm{GaO}_{6}$ units $\left.[60,61]\right)$ where $\mathrm{MO}_{n}$ groups of greater $n$ dominate for glasses of small $\mathrm{M}_{z} \mathrm{O}$ content. Reduced effects of $\mathrm{TeO}_{4} \rightarrow \mathrm{TeO}_{3}$ transition should occur for oxides $\mathrm{M}_{z} \mathrm{O}$ of even smaller $z$ and/or $N_{\mathrm{MO}}$ (with $z<2 / 3$ and $N_{\text {MO }}<6$ ).

For tellurite glasses with $\mathrm{M}=\mathrm{Nb}$ [36] or V [35] the $\mathrm{TeO}_{4} \rightarrow \mathrm{TeO}_{3}$ transition is strongly reduced. An increasing fraction of $\mathrm{TeO}_{4}$ units with $\mathrm{O}_{\mathrm{T}}$ exists. The $N_{\mathrm{TeO}}$ numbers shown for $\mathrm{V}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses [35] are close to a model B which was suggested [62] according to ${ }^{125} \mathrm{Te}$ NMR results (dotted line dropping down). Only $20 \%$ of the oxygens added act in the sense of model A. V-O-V (or Nb-O-Nb) bridges occur for greater fractions of second oxide [35, 36, 62] which indicate for the second component likewise network-forming character. For these glasses the definitions of $\mathrm{O}_{\mathrm{B}}$ and $\mathrm{O}_{\mathrm{T}}$ atoms become problematic due to coexistence of two network-forming oxides. Decreasing values of $N_{\mathrm{MO}}$ numbers with transitions from $\mathrm{VO}_{5}$ to $\mathrm{VO}_{4}$ units [35, 62] and from $\mathrm{NbO}_{7}$ to $\mathrm{NbO}_{6}$ polyhedra [36] are found with increasing $\mathrm{M}_{z} \mathrm{O}$ content.

Though binary tellurite glasses are also formed with many of the typical glass-forming oxides [63] (not with $\mathrm{SiO}_{2}$ ), structural investigations of such series are rare. Note that in this kind of binary systems stable and metastable immiscibility could occur [64]. Obviously, also for the $\mathrm{B}_{2} \mathrm{O}_{3}-\mathrm{TeO}_{2}$ or $\mathrm{GeO}_{2}-\mathrm{TeO}_{2}$ glasses the higher $\mathrm{M}-\mathrm{O}$ coordination states are realized, thus, with $\mathrm{BO}_{4}$ tetrahedra $\left({ }^{11} \mathrm{~B}\right.$ NMR [65]) or large fractions of $\mathrm{GeO}_{6}$ octahedra (Ge K-edge EXAFS [66]). The fraction of $\mathrm{GeO}_{6}$ octahedra decreases with increasing $\mathrm{GeO}_{2}$ content [66]. It seems that $\mathrm{TeO}_{4}$ tbps dominate the tellurite networks of both glass series independent of the $\mathrm{M}_{z} \mathrm{O}$ content [13, 67]. Model C characterizes this behaviour (solid line in figure 7). If only $\mathrm{TeO}_{4}$ units coexist with the $\mathrm{BO}_{4}$ or $\mathrm{GeO}_{6}$ groups some oxygens of the $\mathrm{MO}_{n}$ groups have to be linked with two Te .

Finally, the effect of $\mathrm{P}_{2} \mathrm{O}_{5}$ is discussed. The analysis is started from the point of view of binary phosphate glasses. Different from B or Ge the P atoms do not increase the number of their oxygen neighbours. Since phosphorus has valency five but forms $\mathrm{PO}_{4}$ tetrahedra one of the oxygens has to form a double bond as found in vitreous $\mathrm{P}_{2} \mathrm{O}_{5}[68,69]$. All O atoms of other oxides added are used to disrupt $\mathrm{P}-\mathrm{O}-\mathrm{P}$ bridges [70], and all oxygens of $\mathrm{P}-\mathrm{O}$ bonds outside these bridges tend to coordinate groups of the second component [71]. $\pi$-bonding in the $\mathrm{PO}_{4}$ units is delocalized on more and more $\mathrm{P}-\mathrm{O}$ bonds not being members of $\mathrm{P}-\mathrm{O}-\mathrm{P}$ bridges [72]. Isolated $\mathrm{PO}_{4}$ units are formed in the limit of full degradation of the phosphate networks [45, 46] with four equivalent $\mathrm{P}-\mathrm{O}$ bonds of bond valency $\sim 1.25$. This compositional point is reached at molar ratio $y=c\left(\mathrm{Te}_{0.5} \mathrm{O}\right) / c\left(\mathrm{P}_{2} \mathrm{O}_{5}\right)$ equal to 3 [70]. In the notation of compositions used above this means tellurite glasses with $40 \mathrm{~mol} \% \mathrm{P}_{2} \mathrm{O}_{5}$ or $c\left(\mathrm{M}_{z} \mathrm{O}\right)=\sim 0.77$. The critical number, $M_{\mathrm{TO}}$, of oxygens available for coordination of each Te is $M_{\mathrm{TO}}=v(y+1) / y(v$-valency of Te) [71]. $M_{\mathrm{TO}}$ is equal to $\sim 5.3$ for $y=3$. Now the calculation of $M_{\mathrm{TO}}$ is extended to glasses of smaller $\mathrm{P}_{2} \mathrm{O}_{5}$ content and $M_{\text {TO }}$ is written in the notation used in equation (3). The $\mathrm{Te}-\mathrm{O}$ coordination number is equal to $M_{\text {TO }}$ if every O atom is either in a $\mathrm{P}-\mathrm{O}-\mathrm{Te}$ or in a $\mathrm{Te}-\mathrm{O}-\mathrm{Te}$ bridge. In this case $N_{\text {TeO }}$ varies with the composition by

$$
\begin{equation*}
N_{\mathrm{TeO}}=4+0.4 c\left(\mathrm{P}_{0.4} \mathrm{O}\right) / c\left(\mathrm{TeO}_{2}\right) \tag{4}
\end{equation*}
$$

The corresponding behaviour of $\mathrm{TeO}_{n}$ units is called model D. The change of $N_{\mathrm{TeO}}$ is shown in figure 7 with the dotted line rising. This behaviour translated into fractions of groups means
one $\mathrm{TeO}_{4}$ is changed to a $\mathrm{TeO}_{5}$ unit for every $\mathrm{PO}_{4}$ unit added. For a greater $\mathrm{P}_{2} \mathrm{O}_{5}$ content $\mathrm{TeO}_{6}$ units should also exist. The experimental $N_{\mathrm{TeO}}$ show a trend according to model D but with values being little smaller than those expected (figure 7). The remaining differences can have several reasons: the $\mathrm{P}_{2} \mathrm{O}_{5}$ contents of the glasses studied possess some uncertainty (cf sections 2 and 3.4). Moreover, $\mathrm{TeO}_{n}$ units are highly asymmetric due to LPE effects. Additional oxygens may persist in 'medium' $\mathrm{Te}-\mathrm{O}$ bonds with lengths greater than 0.23 nm which are not included in the $N_{\text {TeO }}$ values shown in figure 7.

Above it was assumed that all O atoms form either $\mathrm{P}-\mathrm{O}-\mathrm{Te}$ or $\mathrm{Te}-\mathrm{O}-\mathrm{Te}$ bridges. If in fact some O atoms were to coordinate more than two Te (or P ) the $N_{\mathrm{TeO}}$ values should increase more than predicted. This situation could exist if all O neighbours found in 'medium' and 'weak' $\mathrm{Te}-\mathrm{O}$ bonds with lengths up to 0.28 nm were included in the considerations. In contrast, effects which could maintain smaller $N_{\text {TeO }}$ values close to four would be the formation of localized double $\mathrm{P}=\mathrm{O}$ or $\mathrm{Te}=\mathrm{O}$ bonds with oxygens not coordinating second neighbours. The corresponding bond lengths should be clearly shorter than those observed. Significant fractions of such bonds are not detected. The increase of $N_{\text {TeO }}$ for $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses results from the strong effect of $\mathrm{PO}_{4}$ units forcing the $\mathrm{Te}(\mathrm{IV})$ to accept an increased number of O neighbours. In this process the sums $S_{\text {bv }}$ of Te (IV) according to equation (2) [43] are constant where the increase of $N_{\mathrm{TeO}}$ is compensated by an elongation of the $\mathrm{Te}-\mathrm{O}$ bonds.

### 4.2. Structural groups of related crystal structures

The diffraction results contain more information than only Te-O coordination numbers. The $T(r)$ functions reveal details of the $\mathrm{Te}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ correlations up to distances of 0.28 nm . Comparisons with the partial correlation functions calculated for related crystal structures should allow us to extract more features of the glass structures. The geometries of some polyhedra of relevant crystal structures are presented before the comparisons are started. The structural units are named $\mathrm{TeO}_{n+m}$ which means they have $n$ 'strong' and $m$ 'medium' $\mathrm{Te}-\mathrm{O}$ bonds. Since the tek08 and tep02 samples have compositions close to that of vitreous (v-) $\mathrm{TeO}_{2}$ the corresponding $\mathrm{TeO}_{4}$ tbps of the three known $\mathrm{TeO}_{2}$ polymorphs [40-42] are also shown (upper part of figure 8). Strictly speaking, the $\mathrm{TeO}_{4}$ unit is a disphenoid [42]. Only if the corner with the LPE is taken into account can a distorted trigonal bipyramid be imagined. As well as the four oxygens in 'strong' bonds (circles with hatched filling) two 'weakly' bonded oxygens (open circles) also exist. The centre of negative charge of the LPE is located close to the Te site in the triangle formed of Te and the two 'weakly' bonded O . The $\mathrm{TeO}_{4}$ tbps of $\alpha-\mathrm{TeO}_{2}$ [40] possess a high symmetry which is lost for the $\mathrm{TeO}_{4}$ of $\beta$ - [41] and $\gamma-\mathrm{TeO}_{2}$ [42]. The distortions result in unlike lengths of both $\mathrm{Te}-\mathrm{O}_{\mathrm{ax}}$ bonds. The shifts seem to be changes toward the geometry of the $\mathrm{TeO}_{3+1}$ unit which is shown for $\mathrm{K}_{2} \mathrm{Te}_{4} \mathrm{O}_{9}$ [34]. The $\mathrm{TeO}_{3+1}$ unit possesses an O atom (circle filled with dots) of 'medium' bond strength. The $\mathrm{TeO}_{3+1}$ units themselves are understood as transitional groups in the change to real $\mathrm{TeO}_{3}$ tps like that shown for $\mathrm{K}_{2} \mathrm{Te}_{2} \mathrm{O}_{5}$ [34]. With $\mathrm{P}_{2} \mathrm{O}_{5}$ additions, the numbers of O atoms in 'strong' and 'medium' $\mathrm{Te}-\mathrm{O}$ bonds increase in steps of the $\mathrm{TeO}_{4+1}$ and $\mathrm{TeO}_{5}$ units.

The 'strong' bonds of $\mathrm{TeO}_{4}$ tbps are differentiated into two short $\mathrm{Te}-\mathrm{O}_{\text {eq }}$ and two long $\mathrm{Te}-\mathrm{O}_{\mathrm{ax}}\left(\sim 0.19\right.$ and $\sim 0.21 \mathrm{~nm}$ ) while $\mathrm{TeO}_{3}$ units have only short 'strong' bonds (figure 8). This differentiation was successful for the $\mathrm{Te}-\mathrm{O}$ peaks of tellurite glasses from earlier diffraction experiments using also high resolving power [35, 36]. Fractions of $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{3}$ units could be analysed considering the fractions of short and longer bonds, where possible $\mathrm{TeO}_{3+1}$ were related to the $\mathrm{TeO}_{3}$ fraction. The same detailed fit was made for the $\mathrm{Te}-\mathrm{O}$ peaks of the $T(r)$ data in the present study. A similar differentiation of lengths was successful for the tek08, tek12, tek16 and tep02 samples. The procedure results in equal fractions of short




Te atom $\bigcirc$


$\mathrm{K}_{2} \mathrm{Te}_{2} \mathrm{O}_{5} \quad \mathrm{TeO}_{3}$ (trigonal pyramid)


Figure 8. $\mathrm{TeO}_{n}$ polyhedra of related tellurite crystals. Upper part: $\mathrm{TeO}_{4}$ trigonal bipyramids (tbps) known of $\alpha-\mathrm{TeO}_{2}$ [40], $\beta-\mathrm{TeO}_{2}$ [41] and $\gamma-\mathrm{TeO}_{2}$ [42]. Lower part: $\mathrm{TeO}_{3+1}$ units in $\mathrm{K}_{2} \mathrm{Te}_{4} \mathrm{O}_{9}$ [34] and $\mathrm{TeO}_{3}$ trigonal pyramids (tps) in $\mathrm{K}_{2} \mathrm{Te}_{2} \mathrm{O}_{5}$ [34], as well as $\mathrm{TeO}_{5}$ units in $\mathrm{P}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ [31] and $\mathrm{TeO}_{4+1}$ units in $\mathrm{P}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ [32]. Circle filling denotes O atoms in 'strong' (hatched), 'medium' (dotted) and 'weak' (no filling) Te-O bonds with distances $r_{\mathrm{TeO}}<0.23 \mathrm{~nm}$, $0.23 \mathrm{~nm}<r_{\mathrm{TeO}}<0.26 \mathrm{~nm}$ and $0.26 \mathrm{~nm}<r_{\mathrm{TeO}}<0.32 \mathrm{~nm}$ where the thick solid lines accentuate the shortest 'strong' bonds. Bond lengths are given in picometres.
and long bonds (tables 2, 3). But the increase of the fraction of shorter bonds as expected for an increasing number of $\mathrm{TeO}_{3}$ units with increasing $\mathrm{K}_{2} \mathrm{O}$ content in $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses is not found. This poor resolution can be due to the great fraction of $\mathrm{TeO}_{3+1}$ which show more varieties of conformations than the $\mathrm{TeO}_{3}$ tps. Also the $\mathrm{TeO}_{4}$ units might have stronger distortions with the higher network connectivity in glasses of little modifier content. The results reported before $[35,36]$ were obtained for glasses of higher modifier content $c\left(\mathrm{M}_{z} \mathrm{O}\right)$.

The $\mathrm{Te}-\mathrm{O}$ bonds in the $\mathrm{TeO}_{5}$ and $\mathrm{TeO}_{4+1}$ units of the $\mathrm{P}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ [31] and $\mathrm{P}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ [32] crystals do not allow us to classify the units into types with definite numbers of short and long bonds. Units of other distortions than those shown in figure 8 also exist in these crystals. Thus, already the $\mathrm{TeO}_{n}$ units of the crystals show that model D can give only an approximate description of $N_{\text {TeO }}$ behaviour due to geometrical variations with an intermixing of short and long 'strong', 'medium' and 'weak' $\mathrm{Te}-\mathrm{O}$ bonds. The shapes of the $\mathrm{Te}-\mathrm{O}$ peaks indicate a non-continuous behaviour. The Te-O peaks of the glasses tep02, tep08, tep14 and tep19 (figures 4,6 ) show the typical narrow component at $\sim 0.19 \mathrm{~nm}$ accompanied by a flat tail on the side of longer distances where the $\mathrm{Te}-\mathrm{O}$ peak of tep 19 is already broader. Different from that the $\mathrm{Te}-\mathrm{O}$ peaks of samples tep27 and tep32 show two clear components at $\sim 0.195$ and $\sim 0.210 \mathrm{~nm}$. A possible explanation of this change is connected with a next deficit of model D: it was assumed that only $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{5}$ units coexist. The latter are needed to compensate for the $\mathrm{PO}_{4}$ tetrahedra. But flexible $\mathrm{TeO}_{n}$ units can form intermediate structures such as $\mathrm{TeO}_{4+1}$. All $\mathrm{TeO}_{n}$ surrounding a $\mathrm{PO}_{4}$ tetrahedron participate in its charge compensation. For


Figure 9. The experimental $T(r)$ functions (dots) of sample tek08 obtained from neutron (a) and x-ray (b) data compared with model $T(r)$ functions (thick solid lines) calculated by use of the SRO of polymorphs $\alpha$ - [40], $\beta$ - [41] and $\gamma-\mathrm{TeO}_{2}$ [42]. Partial correlations: Te-O-thin solid lines; O-O-dash-dotted lines. On top, the $T(r)$ functions of tek08 are compared with those of tep02 sample (solid lines).
small $\mathrm{P}_{2} \mathrm{O}_{5}$ content the compensation is preferably realized with $\mathrm{TeO}_{4+1}$ units. For glasses of $c\left(\mathrm{M}_{z} \mathrm{O}\right)$ content of $\sim 0.55$ the potential to form intermediate $\mathrm{TeO}_{4+1}$ structures is depleted and real $\mathrm{TeO}_{5}$ units occur. Figure 8 shows only one type of the corresponding $\mathrm{TeO}_{4+1}$ and $\mathrm{TeO}_{5}$ units formed in the related crystal structures. Uniform types of polyhedral geometry are not identified. A great variety of $\mathrm{TeO}_{5}$ units should exist in the glass structures where distances of 0.21 nm dominate (cf figures 4 and 8 ).

### 4.3. Comparison of RDFs of selected glasses with those of related crystal structures

The total $T_{N}(r)$ and $T_{X}(r)$ functions of the related crystal structures are calculated in the distance range of SRO and compared with the experimental $T(r)$ results of the samples with compositions close to those of the related crystalline compounds. The $N_{i j}$ and $r_{i j}$ parameters are taken from the crystal structures. Convolutions with the peak shape functions are made to simulate the termination effects of the Fourier transformations which exist in the experimental $T(r)$ data (cf section 3.2) [37,38]. Peak widths $\Delta r_{i j}$ are introduced to simulate glassy disorder and are adjusted to give best agreement of the peaks with those in the model functions. The weighting factors used in the calculations of the model $T(r)$ functions are taken from the glasses whose $T(r)$ data are used for comparison. Use of these factors avoids differences of peak heights which are only due to differences of atomic fractions.

The first comparisons are made for the polymorphs of $\mathrm{TeO}_{2}$ [40-42] with the $T(r)$ data of glass tek08. On top of figure 9 , comparisons are made with the $T(r)$ functions of glass tep 02 which also shows the effects of a small $c\left(\mathrm{M}_{z} \mathrm{O}\right)$ fraction but with $\mathrm{P}_{2} \mathrm{O}_{5}$ instead of $\mathrm{K}_{2} \mathrm{O}$. Differences at 0.155 and 0.255 nm are due to $\mathrm{P}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ distances of the $\mathrm{PO}_{4}$ units in the tep 02 samples. Another difference is a small increase of the $\mathrm{Te}-\mathrm{O}$ bond lengths for tep02. Since $\mathrm{K}_{2} \mathrm{O}$ and $\mathrm{P}_{2} \mathrm{O}_{5}$ have quite different effects on $\mathrm{TeO}_{n}$ networks (section 4.1) possible changes in $T(r)$ for a glass of pure $\mathrm{TeO}_{2}$ are expected in the limits of the $T(r)$ changes of tek08 and tep02 samples. The $\mathrm{Te}-\mathrm{O}$ distances of the $\alpha$-, $\beta$ - and $\gamma$-forms agree with the experimental $\mathrm{Te}-\mathrm{O}$ peaks (figure 9). Best agreement is obtained for $\beta-\mathrm{TeO}_{2}$ whose $T_{\mathrm{TeO}}(r)$ data possess smooth
behaviour with a constant contribution beyond 0.23 nm . On the other hand, the $\mathrm{O}-\mathrm{O}$ peak which belongs to the edges of the $\mathrm{TeO}_{n}$ units is only well reproduced with the $\mathrm{O}-\mathrm{O}$ distances of $\alpha-\mathrm{TeO}_{2}$. Small differences exist for the $\beta$-form. The $\mathrm{TeO}_{4}$ of $\gamma-\mathrm{TeO}_{2}$, however, possess strongly distorted $\mathrm{O}-\mathrm{Te}-\mathrm{O}$ angles which lead to $\mathrm{O}-\mathrm{O}$ distances not being typical for $\mathrm{v}-\mathrm{TeO}_{2}$. Thus, the $\mathrm{TeO}_{4}$ units of the tek 08 glass show small changes of $\mathrm{Te}-\mathrm{O}$ bond lengths if compared with $\alpha-\mathrm{TeO}_{2}$ but good agreement of the internal angles of the $\mathrm{TeO}_{4}$ units with those of $\alpha-\mathrm{TeO}_{2}$.

The $\mathrm{O}-\mathrm{O}$ peaks of the glasses tek08 and tep02 show no special features (except of a small contribution of edges of $\mathrm{PO}_{4}$ tetrahedra at 0.252 nm for tep02). The $N_{\mathrm{OO}}$ numbers for both samples are $\sim 5$ (tables 2 and 3 ) which number is expected for continuous networks of corner-connected $\mathrm{TeO}_{4}$ tbps. Every oxygen atom in a $\mathrm{Te}_{\mathrm{ax}}-\mathrm{O}_{\text {eq }}-\mathrm{Te}$ bridge has five first oxygen neighbours at $\sim 0.280 \mathrm{~nm}$, two in the $\mathrm{O}_{\mathrm{ax}}$ and three in the $\mathrm{O}_{\mathrm{eq}}$ position (cf figure 9). The $\mathrm{O}-\mathrm{O}$ distances with the O neighbours in 'weak' bonds are clearly longer than $0.28 \mathrm{~nm} . N_{\mathrm{OO}}$ obtained from the experiments is a mean number and disorder in the connections of $\mathrm{Te}-\mathrm{O}_{\mathrm{eq}}$ and $\mathrm{Te}-\mathrm{O}_{\mathrm{ax}}$ bonds is expected for a glass. With increasing $\mathrm{K}_{2} \mathrm{O}$ or $\mathrm{P}_{2} \mathrm{O}_{5}$ content the $N_{\mathrm{OO}}$ numbers of the glasses for the peak at 0.28 nm decrease due to disrupture of $\mathrm{Te}-\mathrm{O}-\mathrm{Te}$ bridges or replacement of Te by P positions.

From spectroscopic results of $\mathrm{TeO}_{2}$ glass and crystals other authors [73] suggested most similarity with the structure of $\gamma-\mathrm{TeO}_{2}$ [42]. Also recrystallization of v- $\mathrm{TeO}_{2}$ starts with $\gamma$ $\mathrm{TeO}_{2}$ [73]. The role of small $\mathrm{P}_{2} \mathrm{O}_{5}$ or $\mathrm{K}_{2} \mathrm{O}$ contents of those glasses (tep02, tek08) which are used in the comparisons is not fully clear. But comparisons in [73] were also made with pure and doped $\mathrm{TeO}_{2}$ glasses with no serious changes in the results. On the other hand, from consideration of the network structures of the three $\mathrm{TeO}_{2}$ polymorphs it is suggested that the $\beta$-form of $\mathrm{TeO}_{2}$ has a layer-like network structure also with edge-connections between the $\mathrm{TeO}_{4}$ units. The $\gamma$-form has a 3D-network of corner-connected $\mathrm{TeO}_{4}$ units but with the short $\mathrm{Te}-\mathrm{O}$ bonds in chain orientation. Edge-connections and strong orientations of the units change the $\mathrm{O}-\mathrm{Te}-\mathrm{O}$ angles. Consequently, a network developed likewise in all three dimensions with preferably corner-connected $\mathrm{TeO}_{4}$ tbps as in $\alpha-\mathrm{TeO}_{2}$ is suggested for $\mathrm{v}-\mathrm{TeO}_{2}$ but with some disorder in the $\mathrm{Te}-\mathrm{O}_{\mathrm{ax}}$ and $\mathrm{Te}-\mathrm{O}_{\mathrm{eq}}$ links and, possibly, with small fractions of $\mathrm{TeO}_{4+1}$ and $\mathrm{TeO}_{3+1}$ units.

The next comparisons are made for the $\mathrm{P}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ [31] and $\mathrm{P}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ [32] crystals. The groups in $\mathrm{P}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ are two $\mathrm{PO}_{4}$ tetrahedra, two $\mathrm{TeO}_{5}$ units and a $\mathrm{TeO}_{4+1}$ unit where all oxygens are forming bridges except of an O atom having two 'strong' and an additional 'medium' $\mathrm{Te}-\mathrm{O}$ bond. The structure of this crystal is close to the behaviour of model D . The corresponding $T(r)$ functions (figure 10(a)) show several differences from the $T(r)$ of the glass tep27. Too many $\mathrm{Te}-\mathrm{O}$ bonds have distances of 0.21 nm but there is a deficit of distances of 0.19 nm . The other crystal $\mathrm{P}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ has only $\mathrm{TeO}_{4+1}$ instead of the $\mathrm{TeO}_{5}$ expected according to model D. One $\mathrm{P}-\mathrm{O}$ bond of each $\mathrm{PO}_{4}$ is not a member of a typical $\mathrm{P}-\mathrm{O}-\mathrm{Te}$ bridge but the corresponding oxygens possess two Te neighbours forming only 'medium' and 'weak' bonds. Thus, different from our model assumption the $\mathrm{P}=\mathrm{O}$ double bond is partially localized. The corresponding $T(r)$ functions (figure $10(\mathrm{~b})$ ) show small differences from the $T(r)$ of the glass tep19. The model $\mathrm{Te}-\mathrm{O}$ peak is a little too small and distances are especially missing at 0.22 nm . Both crystal structures show that $\mathrm{P}-\mathrm{O}$ distances less than 0.29 nm do not occur except for the short $\mathrm{P}-\mathrm{O}$ bonds, which assumption was made in the analysis of the $\mathrm{Te}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ correlations (section 3.4).

The two crystal structures show differences from model D (each O has two neighbours) in opposite directions. $\mathrm{P}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ [32] has two oxygens where second neighbours are only in 'medium' $\mathrm{Te}-\mathrm{O}$ bonds while $\mathrm{P}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ [31] has one oxygen with a third neighbour in a 'medium' $\mathrm{Te}-\mathrm{O}$ bond. The comparisons of figure 10 have shown that the $\mathrm{Te}-\mathrm{O}$ peaks of the glasses are found between those of both crystal structures (cf also the $N_{\text {TeO }}$ in figure 7). The


Figure 10. The experimental $T(r)$ functions (dots) of samples tep27 (a) and tep19 (b) compared with model $T(r)$ functions (thick solid lines) calculated by use of the SRO of crystals $\mathrm{P}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ [31] (a) and $\mathrm{P}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ [32] (b). Partial correlations: $\mathrm{P}-\mathrm{O}$-dashed lines; $\mathrm{Te}-\mathrm{O}$ - thin solid lines; O O -dash-dotted lines; $\mathrm{Te}-\mathrm{P}$-short dash lines; $\mathrm{Te}-\mathrm{Te}$-dash-double-dot lines. The vertical arrows indicate if downward, surfeit of distances; if upward, deficiency of distances of the model function in comparison with the experimental results.


Figure 11. The experimental $T(r)$ functions (dots) of sample tek 16 compared with model $T(r)$ functions (thick solid lines) calculated by use of the SRO of crystal $\mathrm{K}_{2} \mathrm{Te}_{4} \mathrm{O}_{9}$ [34]. Partial correlations: Te-O-thin solid lines; O-O-dash-dotted lines; K-O-dashed lines; $\mathrm{Te}-\mathrm{Te}-$ short dash lines; Te-K-dash-double-dot lines. The vertical arrows indicate if downward, surfeit of distances; if upward, deficiency of distances of the model function in comparison with the experimental results.
compositions of both crystalline compounds are close to $c\left(\mathrm{M}_{z} \mathrm{O}\right)$ of $\sim 0.55$. Please remember that the shapes of the $\mathrm{Te}-\mathrm{O}$ peaks of the glasses of these compositions indicate changes of the $\mathrm{TeO}_{n}$ units (section 4.2). It seems that the strong change from $\mathrm{P}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ with $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{4+1}$ units to $\mathrm{P}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ with $\mathrm{TeO}_{5}$ and $\mathrm{TeO}_{4+1}$ units is also reflected in the glass structures with a change from $\mathrm{TeO}_{4+1}$ to $\mathrm{TeO}_{5}$ units. But for the glasses this change appears in a broad compositional interval. $\mathrm{TeO}_{5}$ units appear already for glasses of $\mathrm{P}_{2} \mathrm{O}_{5}$ fractions less than that
of $\mathrm{P}_{2} \mathrm{Te}_{4} \mathrm{O}_{13}$ and a greater number of $\mathrm{TeO}_{4+1}$ units still exists for $\mathrm{P}_{2} \mathrm{O}_{5}$ fractions greater than that of $\mathrm{P}_{2} \mathrm{Te}_{3} \mathrm{O}_{11}$ (cf figure 7).

A last comparison is made for the $\mathrm{K}_{2} \mathrm{Te}_{4} \mathrm{O}_{9}$ [34] crystal (figure 11) where the $T(r)$ data of sample tek 16 are used. The $T(r)$ functions of tek 16 show a surfeit of $\mathrm{Te}-\mathrm{O}$ distances at $\sim 0.22 \mathrm{~nm}$ but deficit of $\mathrm{Te}-\mathrm{O}$ distances at $\sim 0.19$ and $\sim 0.24 \mathrm{~nm}$. This difference might be due to the higher fraction of $\mathrm{TeO}_{4}$ tbps instead of $\mathrm{TeO}_{3+1}$ units in the glass which is expected according to the different compositions of 16 and $20 \mathrm{~mol} \% \mathrm{~K}_{2} \mathrm{O}$ for glass and crystal. Thus, also for the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ system it is shown that the transition to $\mathrm{TeO}_{3}$ units should include the $\mathrm{TeO}_{3+1}$ units. A few additional oxygens have been found at 0.28 nm (table 2). The diffraction results are not sufficient to conclude the existence of oxygens at 0.32 nm which complete the highly distorted $\mathrm{TeO}_{6}$ octahedra formed in the structure of the $\mathrm{K}_{2} \mathrm{Te}_{4} \mathrm{O}_{9}$ [34] crystal.

### 4.4. The amphoteric character of $\mathrm{TeO}_{2}$

The large ranges of glass formation of binary tellurite glasses with additions ranging from alkali oxide to phosphorus pentoxide [63] are due to the great variability of Te (IV) atoms forming different oxygen coordination polyhedra. Their LPEs prevent formation of stable polyhedra of high symmetry (high bond energy). The LPEs enable the Te sites to form links of quite different bond valency. The needs of other atomic partners can be satisfied properly. Addition of a great number of $\mathrm{K}^{+}$ions is accompanied by addition of a comparably small number of oxygen atoms. Formation of a maximum number of $\mathrm{O}_{\mathrm{T}}$ with electron charges less than unity is advantageous for coordination of the $\mathrm{K}^{+}$ions. The O atom added with $\mathrm{K}_{2} \mathrm{O}$ disruptures a $\mathrm{Te}-\mathrm{O}-\mathrm{Te}$ bridge between two $\mathrm{TeO}_{4}$ tbps creating two $\mathrm{O}_{\mathrm{T}}$. The $\mathrm{TeO}_{4} \rightarrow \mathrm{TeO}_{3}$ transition doubles the number of $\mathrm{O}_{\mathrm{T}}$ with

$$
\begin{equation*}
2 \mathrm{TeO}_{4 / 2}+\mathrm{O}^{2-} \rightarrow 2\left(\mathrm{TeO}_{3 / 2} \mathrm{O}\right)^{-} \rightarrow 2\left(\mathrm{TeO}_{1 / 2} \mathrm{O}_{2}\right)^{-} \tag{5}
\end{equation*}
$$

Writing $\mathrm{O}_{n / 2}$ means oxygen shared in bridges while full O are in terminal positions. The transitions seem to be more complicated if O atoms in 'medium' and 'weak' $\mathrm{Te}-\mathrm{O}$ bonds are taken into account. These bonds allow the formation of various transitional groups. It is also emphasized that the large $\mathrm{K}^{+}$ions expand the network. A new medium-range order distance appears which is expressed as the first peak at $\sim 13 \mathrm{~nm}^{-1}$ in the $S_{N}(Q)$ factors or the prepeak in the $S_{X}(Q)$ factors (figure 3). This peak grows with increasing $\mathrm{K}_{2} \mathrm{O}$ content. The small remaining number of network links limits glass formation in the $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ system.

A TeO $4_{4} \rightarrow \mathrm{TeO}_{3}$ transition is still profitable for glasses with $\mathrm{Al}^{3+}$ and $\mathrm{Ga}^{3+}$ ions (figure 7). Certainly, the $\mathrm{O}_{\mathrm{T}}$ form $\mathrm{Te}-\mathrm{O}_{\mathrm{T}}-\mathrm{M}$ bridges in this case and are not shared between several M neighbours as needed for $\mathrm{K}^{+}$ions. Step by step, the $\mathrm{TeO}_{4} \rightarrow \mathrm{TeO}_{3}$ transition is reduced if $\mathrm{M}^{\nu+}$ ions of higher valency and smaller dimension are added. High numbers of $\mathrm{O}_{\mathrm{T}}$ become disadvantageous. Also the second oxides show glass forming abilities which are expressed in the existence of the $\mathrm{M}-\mathrm{O}-\mathrm{M}$ bridges. As discussed before most M atoms are variable in forming mixtures of different $\mathrm{MO}_{n}$ polyhedra. This ability is useful because $\mathrm{Te}-\mathrm{O}_{\mathrm{eq}}$ and $\mathrm{Te}-\mathrm{O}_{\mathrm{ax}}$ bonds of $\mathrm{TeO}_{4}$ tbps are not equivalent to each other $\left(\mathrm{Te}-\mathrm{O}_{\mathrm{eq}}\right.$ is stronger than $\left.\mathrm{Te}-\mathrm{O}_{\mathrm{ax}}\right)$ and need different bond partners. The bond valence in $\mathrm{BO}_{4}$ or $\mathrm{GeO}_{6}$ polyhedra is less than unity. Such bonds can be balanced either in bridges with strong $\mathrm{Te}-\mathrm{O}_{\mathrm{eq}}$ bonds or in sharing corners with two $\mathrm{Te}-\mathrm{O}_{\mathrm{ax}}$ bonds. These needs might be problematic with stiff $\mathrm{SiO}_{4}$ units in the formation of a $\mathrm{SiO}_{2}-\mathrm{TeO}_{2}$ glass which is not known to be prepared so far though ternary $\mathrm{TeO}_{2}-$ $\mathrm{B}_{2} \mathrm{O}_{3}-\mathrm{SiO}_{2}$ glasses exist [74]. From this point of view it is interesting that $\mathrm{PO}_{4}$ tetrahedra are well incorporated in tellurite networks. Though the fraction of $\pi$-bonding in the $\mathrm{P}-\mathrm{O}$ bonds of isolated $\mathrm{PO}_{4}$ tetrahedra is distributed to all four bonds [71] its strength can be split according to the needs of the neighbouring $\mathrm{TeO}_{n}$ units. The addition of a small number of $\mathrm{P}^{5+}$ ions is
accompanied by the addition of a comparably great number of oxygen atoms. The response of $\mathrm{Te}(\mathrm{IV})$ atoms is an increase of $N_{\mathrm{TeO}}$ because $\mathrm{P}^{5+}$ ions require a small number (four) of oxygen neighbours but each with a great charge of $\sim 1.25$ electrons. In the competition for the electron charge $\mathrm{TeO}_{2}$ loses to $\mathrm{P}_{2} \mathrm{O}_{5}$ (tellurium acts as a Lewis base). $\mathrm{P}_{2} \mathrm{O}_{5}$ realizes its optimum structure: four-connected $\mathrm{PO}_{4}$ units fixing 1.25 electrons in each $\mathrm{P}-\mathrm{O}$ bond instead of three-connected $\mathrm{PO}_{4}$ units with the fourth corner forming a $\mathrm{P}=\mathrm{O}$ double bond. $\mathrm{TeO}_{2}$ has to accept additional oxygen with deficit of electrons with

$$
\begin{equation*}
\mathrm{PO}_{3 / 2} \mathrm{O}+\mathrm{TeO}_{4 / 2} \rightarrow\left(\mathrm{PO}_{4 / 2}\right)^{-}+\left(\mathrm{TeO}_{5 / 2}\right)^{+} \tag{6}
\end{equation*}
$$

The $\mathrm{Te}(\mathrm{IV})$ atoms seem not to resist this change too much. Anyway, strongly distorted $\mathrm{TeO}_{6}$ octahedra are known in the structure of pure $\mathrm{TeO}_{2}$ (glass and crystal, cf figure 8). Little alteration is needed. The units change to octahedra with the LPEs being sterically less effective. A greater number of 'strong' $\mathrm{Te}-\mathrm{O}$ bonds appears, however, with greater bond lengths.

The changes of the effects of the LPE ( $5 \mathrm{~s}^{2}$ electrons) for $\mathrm{Te}^{4+}$ can be compared with the effects of the LPE ( $6 s^{2}$ electrons) for $\mathrm{Pb}^{2+}$ except that the greater $\mathrm{Pb}^{2+}$ ions have eight oxygen neighbours. $\mathrm{A}_{\mathrm{PbO}}^{4}$ tbp as part of a strongly distorted $\mathrm{PbO}_{8}$ polyhedron is formed in the structure of the $\mathrm{PbSiO}_{3}$ crystal [75]. The oxygen neighbours of the longer $\mathrm{Pb}-\mathrm{O}$ bonds have distances of $\geqslant 0.30 \mathrm{~nm}$. The structure of a $\mathrm{PbV}_{2} \mathrm{O}_{6}$ crystal [76] shows already a less distorted $\mathrm{PbO}_{8}$ polyhedron. Finally, the distortions of $\mathrm{PbO}_{8}$ polyhedra are lost in the structure of $\mathrm{PbP}_{2} \mathrm{O}_{6}$ [77] with the LPE not being sterically active. Here also the greater number of available oxygens forces the $\mathrm{PbO}_{8}$ polyhedra to avoid distortions. The same change is detected for the $\mathrm{Pb}-\mathrm{O}$ environments in the corresponding $\mathrm{PbO}-\mathrm{SiO}_{2}, \mathrm{PbO}-\mathrm{V}_{2} \mathrm{O}_{5}$ and $\mathrm{PbO}-\mathrm{P}_{2} \mathrm{O}_{5}$ glasses [78]. The $\mathrm{Pb}-\mathrm{O}$ environments were found to depend on the species M of second oxide $\mathrm{M}_{z} \mathrm{O}$.

## 5. Conclusions

Three advantageous circumstances have been applied in a diffraction study of the SRO of tellurite glasses: results of neutron and x-ray diffraction experiments are combined (contrast variation). Both experiments were performed using high resolving power ( $Q_{\max }$ of 400 or $280 \mathrm{~nm}^{-1}$ with neutrons from a spallation source or high-energy x-ray photons from a synchrotron). The $\mathrm{P}-\mathrm{O}$ or $\mathrm{K}-\mathrm{O}$ bond lengths of the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ or $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses do not interfere with the $\mathrm{Te}-\mathrm{O}$ first-neighbour peaks. Moreover, first $\mathrm{P}-\mathrm{O}$ distances except the short $\mathrm{P}-\mathrm{O}$ bonds appear only beyond 0.29 nm . So the $\mathrm{Te}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ correlations are approximated by Gaussian fitting of the x-ray and neutron correlation functions up to lengths of 0.28 nm . In the case of $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses reasonable assumptions are made for the $\mathrm{K}-\mathrm{O}$ first-neighbour peaks at $\sim 0.275 \mathrm{~nm}$.
$\mathrm{Te}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ coordination numbers of four and five are found for the glasses of compositions close to $\mathrm{TeO}_{2}$ which indicates formation of a three-dimensional network of preferably corner-connected $\mathrm{TeO}_{4}$ tpbs. The network groups are $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{3}$ units in $\mathrm{K}_{2} \mathrm{O}-$ $\mathrm{TeO}_{2}$ glasses and $\mathrm{TeO}_{4}$ and $\mathrm{TeO}_{5}$ units in $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses. Additional $\mathrm{Te}-\mathrm{O}$ neighbours are determined in an interval $0.23 \mathrm{~nm}<r<0.29 \mathrm{~nm}$. For $\mathrm{K}_{2} \mathrm{O}-\mathrm{TeO}_{2}$ glasses existence of $\mathrm{TeO}_{3+1}$ units is suggested. For the $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses distorted $\mathrm{TeO}_{6}$ polyhedra exist independent of the $\mathrm{P}_{2} \mathrm{O}_{5}$ content.

The unusual increase of the $\mathrm{Te}-\mathrm{O}$ coordination number in $\mathrm{P}_{2} \mathrm{O}_{5}-\mathrm{TeO}_{2}$ glasses is due to the strong preference of the $\mathrm{PO}_{4}$ tetrahedra to form equivalent $\mathrm{P}-\mathrm{O}$ bonds typical for orthophosphate $\left(\mathrm{PO}_{4 / 2}\right)^{-}$units. The formation of $\mathrm{TeO}_{4+1}$ and $\mathrm{TeO}_{5}$ units compensates for the surfeit of oxygen and deficiency of electron charge. The increase of the Te-O coordination state is realized by reduction of the steric effect of the LPE where with $\mathrm{P}_{2} \mathrm{O}_{5}$ additions a change from highly distorted $\mathrm{TeO}_{6}$ octahedra in $\mathrm{TeO}_{2}$ to less distorted $\mathrm{TeO}_{6}$ with higher fraction of
$\mathrm{Te}-\mathrm{O}$ distances in the range of 'strong' bonds occurs. In this process the number of $\mathrm{Te}-\mathrm{O}$ distances of $\sim 0.21 \mathrm{~nm}$ exceeds those of $\sim 0.19 \mathrm{~nm}$.

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[^0]:    ${ }^{\mathrm{a}}$ These values are fixed in the fits.

